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# Implementations of Manipulator Control Computation on Conventional and Dataflow Multiprocessors

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# IMPLEMENTATIONS OF MANIPULATOR CONTROL COMPUTATION ON CONVENTIONAL AND DATAFLOW MULTIPROCESSORS

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#### I. Introduction

Dynamic control of manipulators involves real-time calculation of the desired forces or motor torques to allow manipulator to follow the required trajectory[1]. These calculations are normally based on the manipulator dynamic equations and the feedback information about the actual motion of manipulator. To achieve convergence of the control algorithm may require sampling rates greater than 60 Hz, with the upper limit being determined by the mechanical resonance. Given this and the high degree of nonlinear characteristics of manipulator the computation load on the controller is substantial, and has in the past required an expensive minicomputer or even a super-minicomputer.

An alternative approach is to decompose the computation load of manipulator dynamic control into a number of tasks which will be performed by inexpensive multiprocessors concurrently [2][3].

Success of such an approach requires an optimal algorithm to assign tasks to respective processors and an efficient configuration of multiprocessor system to support concurrent computation.

This paper presents a number of implementations of the control computation of a manipulator on multiprocessor computer systems. Our research lies in exploring implicit parallel programming schemes for real-time control and as such is a departure from the more usual explicit solution techniques in the literature.

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#### II. The Recursive Newton-Euler Equations

There are a number of ways to formulate the dynamic equation of manipulator motion, two main approaches that are widely used to systematically derive the dynamic model of a manipulator are the Lagrange-Euler(LE) formulation and the Newton-Euler(NE) formulation [4].

The LE formulation generates a set of closed form differential equations to describe motion. The computation method of the LE equations involves many matrix multiplication and is computationally inefficient.

The NE formulation yields a computationally efficient set of forward and backward recursive equations of motion. This algorithm is the fastest and the most efficient of existing algorithm for dynamic control computation [4].

The Newton-Euler equations are based on Newton's second law

$$\mathbf{F}_{i} = \mathbf{m}_{i} \mathbf{a}_{i}$$

and Euler's equation

$$\mathbf{N_i} = \mathbf{I_i} \dot{\mathbf{w_i}} + \mathbf{w_i} \times (\mathbf{I_i} \mathbf{w_i})$$

Furthermore, recursive Newton-Euler equations are derived with nine equations for each link [1].

where:  $A_i^{i-1}$  and  $I_i$  are 3x3 matrices,  $q_i$ ,  $q_i$ ,  $\tau_i$ ,  $m_i$  and  $b_i$  are scalars, the rest are 3x1 vectors.

The manipulator configuration chosen is a popular ASEA IRb-6 robot arm which has five degrees of freedom, so there are in total 45 equations.

## III. Explicit Parallel Implementations on a Shared Memory Multiprocessor

In these implementations, the Pascal programs augmented <u>explicitly</u> with the synchronisation primitives from the parallel programming library of Encore Multimax, a shared-memory multiprocessor system with six processors, is used to implement the computation of manipulator dynamic control equations.

The primitives used were fork, *spinlock*, *spinunlock*, *fbarrier\_init*, *fbarrier* and the memory allocation directive *share*[5], where fork is used to create a new process. The new process (the child) is an exact copy of the calling process (the parent) except for the child process has an unique process ID. In the program, one process runs on one physical processor. Spinlock and spinunlock are used where necessary to provide exclusive access to the data structures located in a shared memory. Fbarrier\_init and fbarrier are used to synchronise the parallel processes on each iteration of the control loop.

<u>Decomposition of the computing load into tasks</u> The decomposing of the computing load is the first and important step in the application of parallel processing. If we split the computing load into coarse grains, only a few tasks can be performed concurrently. On the other hand, if the grains are too small, the data transfer activities between the processors (hence the operating system overhead) will increase. This effect will lead to the performance degradation.

After a substantial number of experiments[15], we finally partitioned the recursive Newton-Euler equations into 51 tasks. A task graph was sketched to represent the ordering constraint arising from the data dependencies between the tasks and is shown in Figure 1, where task 0 and 52 are dummy tasks, representing enter node and exit node respectively.

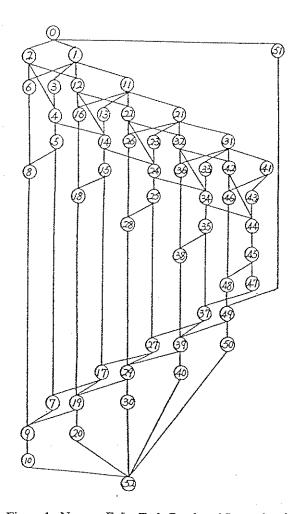


Figure 1: Newton-Euler Task Graph and Dependencies

In a task graph, there is a longest path called critical path whose path length is defined as follow:

$$t_{cr} = \max_{k} \sum_{i \in \phi_k} t_i$$

where  $\phi_k$  represents the kth path from the entry node to the exit node.

The critical path length play a principal role since once the critical path length is determined, no matter what scheduling is used and how many processors will be employed, the execution time will be not shorter than this critical path length.

Using UNIX -gprof, we can estimate the execution time of each task, furthermore, the critical path length can be inferred:

the critical path: 0->2->12->22->32->42->44->45->47->37->39->29->19->9->10->52

the critical path length = 48.354 (sec) (40,000 iterations)

A task can not start until all of its predecessors are completed. Threshold variables are used to determine when a task is ready to be executed and that task is then scheduled. Two methods have been employed to schedule tasks. One is dynamic scheduling and the other is static scheduling.

<u>Dynamic scheduling</u> For dynamic scheduling, all of the processors share a common task queue which is located in a shared memory and the tasks are scheduled at run-time. If we denote:

- T be a set of tasks, i.e.  $T=(T_0, T_1, ..., T_i, ..., T_n, T_{n+1})$ , where  $T_0$  and  $T_{n+1}$  are dummy tasks, representing the enter node and the exit node in a task graph, respectively.
- P be a set of processors, i.e.  $P=(P_1,..., P_j, ..., P_m)$ ; then the dynamic scheduling can be described as the following steps:
  - 1. Initially, T<sub>0</sub> is put into the queue, and a shared variable remaining\_tasks is set to equal to NoOfTasks;
  - 2. P<sub>j</sub> checks the variable remaining\_tasks: IF remaining\_tasks=0, then go to step 4, ELSE go to step 3;
  - 3.  $P_j$  reads a task  $T_i$  from the queue, IF  $T_i <> T_{n+1}$ , i.e.  $T_i$  is not the exit node, then  $P_j$  performs  $T_i$ . After completing  $T_i$ ,  $P_j$  checks the thresholds of successors of  $T_i$  and put any task with threshold equal to its NoOfPred (No Of Predecessors) into the queue. go to step 2; ELSE  $P_i$  sets the variable remaining\_tasks=0, and go to step 2;
  - **4.** stop.

Spinlock is used to guarantee that only one processor can access to the queue at each time.

The advantage of dynamic scheduling is that it is simple to programme, and avoids manual work such as mapping tasks to specific processors. The drawback is that a processor spends quite a long time on scheduling and spinlock/spinunlock.

Static scheduling For static scheduling, tasks are allocated to specific processors. The order in which the tasks are executed on a given processor is predetermined. Tasks wait until the predecessors have finished before executing. In this case, the task itself monitors the threshold rather than being explicitly scheduled by a predecessor. In the program, we use DHLF/MISF (Dynamic High Level First / Most Immediate Successive First) [16] method to generate a task order for each processor and then directly map the tasks to specific processors. If a task and its

predecessor are allocated to the same processor, then the No Of Predecessors of this task can be reduced by 1.

The scheduling time for static scheduling has been greatly reduced, however, this method involves substantial manual work to map tasks to specific processors.

The results in Table 1 are for the dynamic control routine. It can be see that for dynamic scheduling, using one processor, the execution time is worse than that of the sequential scheme, using more than two processors, only a slight speedup can be achieved. This is because that processors spend a significant amount of time in locks. It also can see that for the static scheduling, the moderate speedup has been achieved by using several processors.

	scheduling	processor number	execution time (sec)	speedup
sequential			142.3	
parallel	dynamic	1	186.9	
		2	130.7	1.09
		3	104.2	1.37
		4	87.2	1.63
		5	80.8	1.76
	static -	1	142.3	1.00
		2	84.7	1.68
		3	66.3	2.15
		4	61.3	2.32
		5	60.0	2.37

Table 1: Times for Dynamic and Static Implementations (40000 iterations)

### IV. Implicit Parallel Implementations in Sisal

Sisal is a functional language which has been targeted at a wide variety of systems including current generation multiprocessors such as the Encore Multimax and research dataflow machines [6][7]. The multi-targeting feature is accomplished by compiling Sisal to an intermediate language IF1. The IF1 representation is then compiled to the appropriate target instruction set. The textual form of Sisal, in terms of control structures and array representations, provides a relatively easy transition for those familiar with imperative languages. The optimising Sisal compiler (OSC) from Colorado and Lawrence Livermore National Laboratories yields performance competitive with FORTRAN.

In Sisal program, there two forms of Loop expression, one is of the form:

for initial
 index:=lowest\_index;
 variable:=initial\_value;
while index<=highest\_index repeat
 index:=old index + 1;
 variable:=function1(old index, old variable);
return array of variable
end For</pre>

Another form of Loop expression is:

```
for index in lowest_index, highest_index
  variable:=function2(index);
return array of variable
end For
```

The first one performs sequential loop in which one iteration depends on the results of previous iteration. The second form may be used when there are no data dependencies between iterations, this makes it is possible to execute several loops in parallel.

<u>Sisal on a Conventional Shared Memory Multiprocessor</u> As we know, the dynamic control of manipulator involves calculating nine equations for each link. The data dependencies among nine equations and between two links are so strong that it is difficult to write the calculation program in second form of parallel Sisal loop. The manipulator program expressed in Sisal is presented below. It can be seen that there are no directives as to how the tasks should be scheduled.

```
vector = record[x,y,z:real];
      matrix = record[n,o,p:vector];
function VAV(a,b:vector returns vector)
                                            %vector + vector
    c:=record vector[x:a.x+b.x;y:a.y+b.y;z:a.z+b.z]
  in c
  end let
end function
function dynamic_control(z0:vector;dq,ddq,m,bo:array[real];
        po.s:array[vector];Tm,Tm_1,Im:array[Matrix] returns
                              w,dw,v,dv,dcv,Fe,Ne,fc,nc,t)
 wi,dwi,dvi,dcvi,Fej,Nej:=
  for initial
     link:=0;
     wi:=record vector[x:0.0;y:0.0;z:0.0];
  while link<=4 repeat
     link :=old link+1;
     wi,dwi,dvi,dcvi,Fei,Nei:=
     if motion[link]=1 then
                                                         %rotation
       let
         %compute angular velocity
        zdq:=SMV(dq[link],z0);
        value01:=VAV(old wi,zdq);
         w1:=MMV(Tm_1[link],value01);
         %compute external moment - Ne1
       in w1,dw1,dv1,dcv1,Fe1,Ne1
       end let
    else
                                                        %translation
         %compute angular velocity
         w1:=MMV(Tm_1[link],old wi);
         %compute external moment - Ne1
       in w1,dw1,dv1,dcv1,Fe1,Ne1
       end let
     end if
     returns array of wi
```

```
array of Nei
end for;
w,dw,dv,dcv,Fe,Ne:=array_setl(wj,0),
:
array_setl(Nej,0)
:
:
in w,dw,dv,dcv,Fe,Ne,fc,nc,t
end let
end let
end function
```

The Sisal compiler OSC (Optimising Sisal Compiler) exploits only the parallelism in for ... in loop for shared-memory machines. Procedural level concurrency of the type found in the manipulator control program is not currently exploited as can be seen from the results in Table 2 (It is hard to work out the execution time for the dynamic control routine alone since Sisal optimise eliminates the routines as 'dead code' if their results are not used). It can be observed however that the run times for Sisal on a conventional multiprocessor compare favourably with the Pascal implementations. The execution time slightly increasing with additional processors is caused by the operating system overhead.

	execution time (sec)			
processor number	whole program	outside dynamic control routine	dynamic control routine (infer)	
1	291.8	175.3	116.5	
2	308.5	189.3	119.2	
3	312.5	190.9	121.6	
4	316.1	196.4	119.7	

Table 2: Times for Sisal on a Conventional Multiprocessor (40000 iterations)

Sisal on a Dataflow Multiprocessor The dataflow model has been introduced to exploit the maximum parallelism inherent in algorithms since the early 1970s. Dataflow microprocessors are commercially available and other microprocessors such as the Inmos transputers may be used as dataflow processors[14]. Unlike the conventional control-flow model the course of a computation is determined solely by the availability of data, therefore, the dataflow model can avoid most of problem existing in the conventional multiprocessor system, such as memory conflict, side effects, etc.

Dataflow programs are represented by a directed graph where the arcs denote paths over which data travels and the node the computational function (instruction operation). A node 'fires' as soon as all its operands arrive on all its input arcs. When the node fires, results are transmitted to successor nodes in data packets called token and these nodes will cause further firings. Potentially many nodes may be eligible to fire in parallel.

The hardware of the dataflow machine studied (CSIRAC II) consists of a homogeneous array of processing-elements or processors interconnected by a modulo 4 multi-stage interconnection network (MIN). The graph describing the computation to be performed is partitioned and the partitions distributed to the processing elements [8][9][10]. In CSIRAC II, a processing element consists of two main functional units (Figure 3). If the destination node is monadic, the token can be directly passed to the evaluation unit; If the destination node is diadic, then the matching unit retains the token and processes the next token; the retained token is retrieved when its partner arrives. In the evaluation unit the node function is evaluated and the results are

dispatched through the communication network to their destinations[11].

The CSIRAC II development environment provides a simulator for detailed language studies. In the simulator, the discrete time increment, nominally 10 nsec, is used to calculate all execute time. The transmission time of communication network is assumed as 100 nsec per 128 bit word and the relevant communication path is modelled as being busy for the entire period of token transmission. The default communication latency is 500 nsec although this may be varied. Pipelining within processing elements is not modelled directly but approximated by commencing the processing of tokens a time equal to half the transmission time after the token has been dispatched. The rate for reading tokens from and written tokens to queues is assumed as 50 nsec per word and the time for tokens to perform the matching operation is assumed as a very conservative 500 nsec plus another 500 nsec for each further search or token storage. The basic node evaluation time is 100 nsec with the more complex node evaluation time set to appropriately long time [18][19]. The execution time of a program running on the simulator is calculated based on above assumption. The simulator also generates a number of graphics for performance analysis [8].

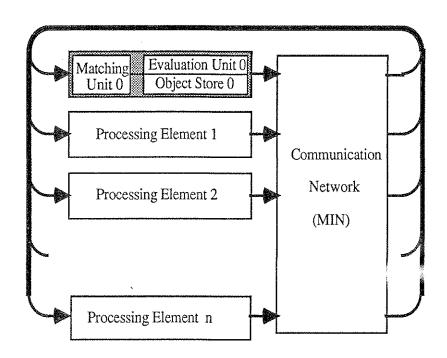


Figure 3: CSIRAC II Organisation

For CSIRAC II, Sisal programs are compiled by the front end of OSC into IF1(an intermediate form). The IF1 is then translated into i2, an intermediate target language which directly represents a data flow graph [9][13].

The set of graphs in Figure 4 shows the machine activity during the simulation. Where graph 4-a shows the number of unmatched tokens and transited tokens; Graph 4-b shows the maximum, minimum and average number of active processing elements during each time step; Graph 4-c shows the activity of processing elements accessing the object store; Graph 4-d shows the work-load distribution, a dark spot indicates that processing element is active [8].

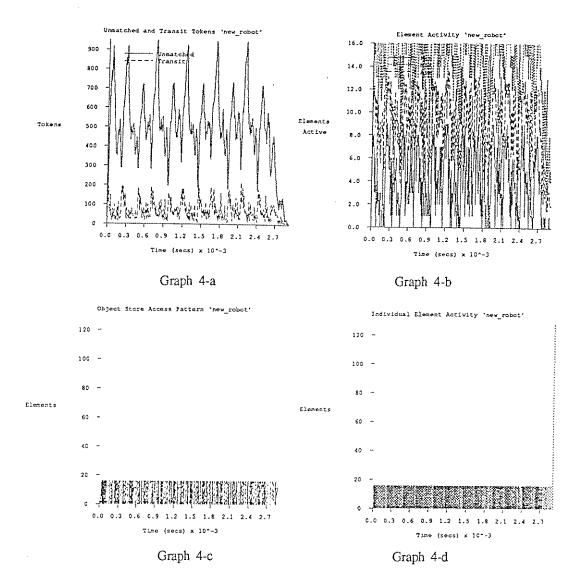


Figure 4: Machine Activity During the Simulation

The following Table 3 indicates the execution time of whole simulation program for ten iterations by using different number of processing element:

Table 3: Runtime for SISAL on dataflow (10 iterations)

processing element number	execution time (ms)	speedup
1	27.506	
2	14.472	1.91
8	4.386	6.27
16	2.923	9.41
32	2.329	11.81
64	2.149	12.80
128	2.085	13.19

#### V. Conclusion

We have investigated several computation models for the dynamic control of a manipulator. As we know, program parallelism involves the partition of a computing load. In theory, if we wish to speedup our program, we should cut down the critical path length, to do so, we should produce a fine grained program to exploit low level parallelism in tasks, further reducing critical path. However, if the grains are too small, there will be substantial overhead associated with coordinate processes, the actual critical path length will increase. Therefore, the potential gain from parallelism will be overwhelmed by this lengthening of the critical path. This can be seen from our shared- memory schemes, where, each processors can directly access a data structure located in shared memory which also can be accessed by all other processors. In order to avoid this contest, some method is required for ensuring mutual exclusion. The method we use here is spinlock. However, the spinlock can degrade the performance of parallel processing since it can slow down processors doing useful work. This is why we only exploit medium granularity for our shared-memory schemes and only a slight speedup has been achieved by using dynamic scheduling and a moderate speedup by using static scheduling. Although part of the software scheduling can be replaced by hardware, a certain effects could be received, only a limited speed-up can be achieved since a limited number of processors could be employed.

The dataflow model of computation deviates from the conventional control flow in that the execution of an instruction is solely based upon the availability of its operands. The instructions in the data flow model of computation do not impose any constrains on sequencing except the data dependencies in the program. The advantage of the data flow approach over the conventional control flow method stems from the inherent parallelism embedded at the instruction level. This allows efficient exploitation of the fine-grain parallelism in an application program and can make the critical path length of the program minimum, which is suitable to parallelise the computation of dynamic control of a manipulator. Sisal <u>automatically</u> partitions the program into very fine-grained tasks (instruction level) and their data dependencies. The CSIRAC II dataflow machine uses a dynamic scheduling policy very similar to the one used in the Pascal based scheme. The simulation results demonstrate the potential and advantage of dataflow machine to resolve a complicated and high performance real time control problem such as manipulator dynamic controls.

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